# MARK SCHEME for the October/November 2011 question paper for the guidance of teachers 

## 4024 MATHEMATICS (SYLLABUS D)

4024/21 Paper 2, maximum raw mark 100

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

- Cambridge will not enter into discussions or correspondence in connection with these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2011 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

| Page 2 | Mark Scheme: Teachers' version | Syllabus | Paper |
| :---: | :---: | :---: | :---: |
|  | GCE O LEVEL - October/November 2011 | 4024 | 21 |

## Abbreviations

| cao | correct answer only |
| :--- | :--- |
| cso | correct solution only |
| dep | dependent |
| ft | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| www | without wrong working |
| soi | seen or implied |


| Qu | Answers | Mark | Part marks |
| :---: | :---: | :---: | :---: |
| 1 | (a) 3.64 <br> (b) $8.24-8.28$ <br> (c) $24.2,24.3$ | 2 <br> 2 ft <br> 3ft | M1 for $10 \tan 20$ oe <br> M1 for $10(\tan 50-\tan 20)$ oe <br> M1 for $(P C=) \frac{10}{\cos 20}$ oe $(=10.64)$ and <br> M1 for their (a) $+10+$ their $P C$ |
| 2 | (a) $0 \quad-7 / 3$ oe isw <br> (b) $x=1 \quad y=-1 / 2$ oe <br> (c) $\frac{6 p+23}{(p-2)(2 p+3)}$ final Ans <br> (d) $\frac{q+1}{2 q-1}$ final Ans | 2 <br> 3 <br> 3 <br> 3 | B1 for one correct <br> B2 for one correct www or M1 for reaching such as $\begin{aligned} & h x=11,11 x=\mathrm{k}, \text { or } \\ & p y=-22,44 y=q \end{aligned}$ <br> M1 for $\frac{5(2 p+3)-4(p-2)}{(p-2)(2 p+3)}$ soi and <br> A1 for numerator $10 p+15-4 p+8$, condoning one sign error, and correct denominator seen at some stage <br> B1 for $(q-1)(q+1)$ seen and B1 for $(2 q-1)(q-1)$ seen |
| 3 | (a) 60 alternate angles <br> (b) (i) 130 <br> (ii) 310 <br> (iii) 250 <br> (c) (i) Triangles equiangular <br> (ii) 51 | 1 <br> 1 <br> 1 <br> 1ft <br> 1 <br> 3 | ft 360 - (their $(\mathbf{a})+50)$ or their (b)(ii) - their (a) <br> M2 for $\frac{T Q}{85-T Q}=\frac{3}{2}$ oe or M1 for $\frac{T Q}{T R}=\frac{3}{2}$ oe |


| Page 3 | Mark Scheme: Teachers' version | Syllabus | Paper |
| :---: | :---: | :---: | :---: |
|  | GCE O LEVEL - October/November 2011 | 4024 | 21 |


| 4 | (a) (i) $\frac{1}{5}$ oe <br> (ii) 1 oe <br> (b) (i) Correct completion <br> (ii) (a) 0 <br> (b) $\frac{6}{25}$ oe <br> (c) $\frac{1}{25}$ | 1 <br> 1 <br> 2 <br> 1ft <br> 1ft <br> 2 | B1 after up to 3 errors <br> ft from their table <br> Both fts dep on at least B1 scored in (b)(i) <br> B1 for $5 \times 5 \times 5$ soi |
| :---: | :---: | :---: | :---: |
| 5 | (a) Convincing explanation <br> (b) (i) $4(\pi)$ <br> (ii) $\frac{3}{4}$ <br> (c) (i) 75.4 <br> (ii) 45.7 | 1 <br> 1 <br> 2 ft <br> 2 <br> 3 | B1 for $3 \pi$ <br> M1 for $\frac{60}{360} \times \pi \times(\text { their } r)^{2}$ <br> M1 for $1 / 2 \times 6 \times 6 \times \sin 60$ or $1 / 2 \times \pi \times 3 \times 3$ and <br> M1 for their 75.4 - their $1 / 2 \times 6 \times 6 \times \sin 60$ <br> - their $1 / 2 \times \pi \times 3 \times 3$ evaluated |
| 6 | (a) (i) $3: 5$ <br> (ii) 9600 <br> (iii) 20000 <br> (b) (i) 252.48 <br> (ii) $110.8(0)$ <br> (iii) 33.4 | $\begin{aligned} & 1 \\ & 1 \\ & 2 \\ & 1 \\ & 2 \\ & 2 \end{aligned}$ | M1 for $\div$ figs 1125 oe <br> M1 for $395+\mathrm{k} x=3054.20$ soi <br> M1 for $\div$ figs 2395 soi |
| 7 | (a) (i) Congruency case complete www <br> (ii) (a) $\frac{16}{25}$ oe <br> (b) $\frac{3}{25}$ oe | 1 | D1 for common angle of 60 and S1 for $A P=B Q=C R$ or $A R=B P=C Q$ |


| Page 4 | Mark Scheme: Teachers' version | Syllabus | Paper |
| :---: | :---: | :---: | :---: |
|  | GCE O LEVEL - October/November 2011 | 4024 | 21 |


|  | (b) (i) Angle in a semicircle oe <br> (ii) Equal arcs or equal chords subtend equal angles at the circumference <br> (iii) (a) 45 <br> (b) 135 <br> (iv) 98 | 1 2 1 1 $18 t$ 2 | B1 for $A B=B C$ <br> ft $3 \times$ their (a) <br> B1 for an angle correctly identified as $37^{\circ}$, $53^{\circ}$ or $127^{\circ}$ |
| :---: | :---: | :---: | :---: |
| 8 | (a) 8 correct plots joined <br> (b) $5.5-7.5$ <br> (c) (i) Correct line <br> (ii) 1.3 <br> (iii) $B=4 \quad C=5$ <br> (d) (i) Convincing demonstration <br> (ii) Correct completion of graph | 2 2 2 $18 t$ 3 1 1 1 | P1 for at least 5 correct plots joined <br> M1 for a correct tangent <br> L1 for correct freehand line or a ruled line with gradient - 1 or intercept 2 <br> B2 for one correct www or M1 for $2 x-\frac{5}{2 x}=2-x$ soi |
| 9 | (a) 122 working seen www <br> (b) (i) Correct equation derived www <br> (ii) 4.276 and -9.276 final answer | 3 4 | M1 for $\frac{\sin A B C}{11}=\frac{\sin 25}{5.5}$ and further M1 for $\sin A B C=\frac{11 \sin 25}{5.5}$ soi and A1 for 58 or B1 for 180 - their 58 <br> M2 for $\left(12^{2}\right)=x^{2}+(5+x)^{2}-2 x(5+x) \cos 120$ <br> or <br> M1 for $\left(12^{2}\right)=x^{2}+(5+x)^{2}+2 x(5+x) \cos 120$ <br> B3 for one correct or both not or wrongly corrected <br> or <br> B1 for $p=-15$ and $r=6$ and <br> B1 for $q=1653$ or $\sqrt{q}=40.657$.. <br> or <br> B1 for $\left(x+\frac{5}{2}\right)^{(2)}$ and <br> B1 for $\frac{551}{12}=45.916$ or 6.776 |


| Page 5 | Mark Scheme: Teachers' version | Syllabus | Paper |
| :---: | :---: | :---: | :---: |
|  | GCE O LEVEL - October/November 2011 | 4024 | 21 |

\begin{tabular}{|c|c|c|c|}
\hline \& (iii) 93 \& 1ft \& ft from their positive root in (ii) \\
\hline 10 \& \begin{tabular}{l}
(a) Correct histogram \\
(b) (i) \(\begin{array}{lllll}35 \& 65 \& 100 \& 128\end{array}\) \\
(ii) Correct curve \\
(c) (i) (51) \\
(ii) (10) \\
(d) (16.5)
\end{tabular} \& 1
3

1ft

2 ft

2ft \& | H2 for at least 4 correct columns or H1 for 1 correct column |
| :--- |
| For wrong or no vertical scale award SC2 for all heights correct and all widths correct SC1 for all heights correct or all widths correct |
| P2 for 7 correct ft plots or PC2 for 4 correct ft plots and curve or P1 for 4 correct ft plots |
| B1 for reading from the graph at 105 |
| B1 for reading from the graph at 30 | <br>

\hline 11 \& | (a) (i) (a) $(-2,3)$ |
| :--- |
| (b) $(-3,2)$ |
| (c) $(-3,2)$ |
| (ii) (a) $\left(\begin{array}{cc}1 & 0 \\ 0 & -1\end{array}\right)$ |
| (b) $\mathrm{M}_{\mathrm{y}}$ |
| (b) (i) 5 |
| (ii) 5 |
| (iii) (a) $(0,2)$ |
| (b) 307 | \& 1

1 ft
2
1
1
1
1
2
2
2

1 \& | B1 for one coordinate correct |
| :--- |
| B1 for $\sqrt{(4-7)^{2}+(4-8)^{2}}$ |
| M1 for appropriate perpendicular bisectors | <br>

\hline
\end{tabular}

